

# A critical appraisal of NLO+PS matching

Particle Physics Seminar, Zürich

Frank Siegert

Albert-Ludwigs-Universität Freiburg

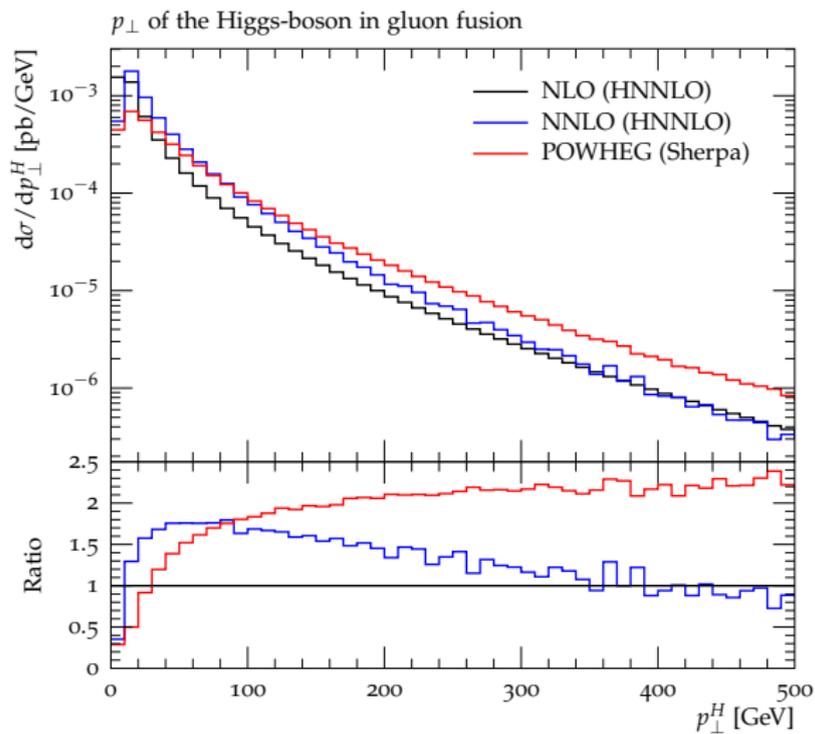


**UNI  
FREIBURG**

Based on

- ▶ [arXiv:1111.1220](https://arxiv.org/abs/1111.1220) (Stefan Höche, Frank Krauss, Marek Schönherr, FS)
- ▶ [arXiv:1008.5399](https://arxiv.org/abs/1008.5399) (Stefan Höche, Frank Krauss, Marek Schönherr, FS)

## Teaser



## A critical appraisal of NLO+PS matching

### Introduction

- Motivation

- Fixed order calculations (NLO)

- Resummation in parton-showers (PS)

### Common formalism for NLO+PS matching

- From fixed order to resummation

- Special cases: POWHEG and MC@NLO

- Subtleties to note

### Results

- NLO+PS uncertainties

- Predictions for  $pp \rightarrow h + \text{jet}$

- Comparison to data for  $W/Z + \text{jet}$

### Conclusions

## Motivation for NLO+PS matching

## Two approaches to higher-order corrections

## Fixed order ME calculation

- + Exact to fixed order
- + Includes all interferences
- +  $N_C = 3$  (summed or sampled)
- + Includes virtual contributions
- Perturbation breaks down in logarithmically enhanced regions
- Only low FS multiplicity

## Parton Shower

- + Resums logarithmically enhanced contributions to all orders
- + High-multiplicity final state
- + Allows for exclusive hadron-level events
- Only approximation for emission ME
- Large  $N_C$  limit



## Goal: Combine advantages

- ▶ Include virtual contributions and **hard QCD radiation** from **NLO ME**
- ▶ Keep **intrajet evolution** provided by the **PS**

## Fixed order calculations (NLO)

## Reminder + Notation: Subtraction method

- ▶ Contributions to NLO cross section:  $\mathcal{B}$ orn,  $\mathcal{V}$ irtual and  $\mathcal{R}$ eal emission
- ▶  $\mathcal{V}$  and  $\mathcal{R}$  divergent in separate phase space integrations  
 ⇒ Subtraction method for expectation value of observable  $O$  at NLO:

$$\begin{aligned} \langle O \rangle^{(\text{NLO})} = & \sum_{\vec{f}_B} \int d\Phi_B \left[ \mathcal{B}(\Phi_B) + \tilde{\mathcal{V}}(\Phi_B) + \sum_{\tilde{i}j} \mathcal{I}_{\tilde{i}j}^{(S)}(\Phi_B) \right] O(\Phi_B) \\ & + \sum_{\vec{f}_R} \int d\Phi_R \left[ \mathcal{R}(\Phi_R) O(\Phi_R) - \sum_{\{ij\}} \mathcal{D}_{ij}^{(S)}(\Phi_R) O(b_{ij}(\Phi_R)) \right] \end{aligned}$$

- ▶ Subtraction terms  $\mathcal{D}$  and their integrated form  $\mathcal{I}$  given e.g. by Frixione-Kunszt-Signer or Catani-Seymour
- ▶ Subtraction defines phase space mappings  $\Phi_R \xrightarrow[r_{\tilde{i}j}]{b_{ij}} (\Phi_B, \Phi_{R|B}^{ij})$

## Resummation in parton-showers

## Factorisation of collinear QCD emissions

Universal factorisation of QCD real emission ME in collinear limit:

$$\mathcal{R}^{ij} \xrightarrow{\text{collinear}} \mathcal{D}_{ij}^{(\text{PS})} = \mathcal{B} \times \left( \sum_{\{ij\}} \frac{1}{2p_i p_j} 8\pi\alpha_s \mathcal{K}_{ij}(p_i, p_j) \right)$$

- ▶ Sum over subterms  $ij$  of the factorisation, e.g. parton lines (DGLAP)
- ▶  $\frac{1}{2p_i p_j}$  from massless propagator  
Evolution variable of shower  $t \sim 2p_i p_j$  (e.g.  $k_\perp$ , angle, ...)
- ▶  $\mathcal{K}_{ij}$  **splitting kernel** for branching  $\tilde{ij} \rightarrow i + j$   
Specific form depends on scheme of the factorisation, e.g.:
  - ▶ Altarelli-Parisi splitting functions
  - ▶ Dipole terms from Catani-Seymour subtraction (in  $N_C \rightarrow \infty$ )
  - ▶ Antenna functions

Radiative phase space factorisation:

$$d\Phi_R \rightarrow d\Phi_B d\Phi_{R|B}^{ij} \stackrel{\text{e.g.}}{=} d\Phi_B \frac{1}{16\pi^2} dt dz \frac{d\phi}{2\pi}$$

## Resummation in parton-showers

## Differential branching probability

$$d\sigma_{\text{branch}}^{\tilde{ij}} = \sum_{f_i=q,g} d\Phi_{R|B}^{ij} \frac{\mathcal{D}_{ij}^{(\text{PS})}}{\mathcal{B}} \quad (\text{Symmetry factors/PDFs ignored})$$

Differential probability for **single** branching of subterm  $ij$  in interval  $d\Phi_{R|B}^{ij}$

## Total “survival” probability of parton ensemble

- ▶ **Integrate single branching** probability down to scale  $t$  in terms of  $t(\Phi_{R|B}^{ij})$
- ▶ Assume **multiple independent** emissions (Poisson statistics)  $\Rightarrow$  **Exponentiation**

$$\begin{aligned} \text{subterm: } \Delta_{\tilde{ij}}^{(\text{PS})}(t) &= 1 - \int d\sigma_{\text{branch}}^{\tilde{ij}} \Theta\left(t(\Phi_{R|B}^{ij}) - t\right) + \dots \\ &= \exp\left\{-\sum_{f_i=q,g} \int d\Phi_{R|B}^{ij} \Theta\left(t(\Phi_{R|B}^{ij}) - t\right) \frac{\mathcal{D}_{ij}^{(\text{PS})}}{\mathcal{B}}\right\} \end{aligned}$$

$$\text{event: } \Delta^{(\text{PS})}(t) = \prod_{\tilde{ij}} \Delta_{\tilde{ij}}^{(\text{PS})}(t)$$

## Resummation in parton-showers

## Cross section up to first emission in a parton shower

$$\langle O \rangle^{(\text{PS})} = \int d\Phi_B \mathcal{B} \left[ \underbrace{\Delta(t_0) O(\Phi_B)}_{\text{unresolved}} + \underbrace{\sum_{\tilde{i}_j} \sum_{f_i} \int_{t_0}^{\mu_F^2} d\Phi_{R|B}^{ij} \frac{\mathcal{D}_{ij}^{(\text{PS})}}{\mathcal{B}} \Delta(t) O(r_{\tilde{i}_j}(\Phi_B))}_{\text{resolved}} \right]$$

Generating events for  $\langle O \rangle^{(\text{PS})}$ 

- ▶ Generate Born ME event  $\mathcal{B}$  at  $\mu_F^2$
- ▶ Generate  $t$  according to survival probability  $\Delta(t)/\Delta(\mu_F^2)$
- ▶ Stop if  $t < t_0$
- ▶ Generate remaining kinematics of the branching  $(z, \varphi)$  according to  $\mathcal{D}_{ij}^{(\text{PS})}/\mathcal{B}$

Features of  $\langle O \rangle^{(\text{PS})}$ 

- ▶ Unitarity:  $[\dots]|_{O=1} = 1$   
 $\Rightarrow$  LO cross section preserved
- ▶ “Unresolved” part:  
 No emissions above cutoff  $t_0$
- ▶ “Resolved” part:  
 Emission between  $t_0$  and  $\mu_F^2$  in PS approximation

## From fixed order to resummation

## Problem

- ▶ Applying PS resummation to  $\mathcal{B}$  event was simple ✓ (for some definition of simple)
- ▶ At NLO, can the same simply be done separately for  $\mathcal{B}, \mathcal{V} + \mathcal{I}, \mathcal{R} - \mathcal{D}$ ?

$$\langle O \rangle^{(\text{NLO})} = \sum_{\vec{f}_B} \int d\Phi_B \left[ \mathcal{B}(\Phi_B) + \tilde{\mathcal{V}}(\Phi_B) + \sum_{\tilde{i}_j} \mathcal{I}_{\tilde{i}_j}^{(S)}(\Phi_B) \right] O(\Phi_B) \\ + \sum_{\vec{f}_R} \int d\Phi_R \left[ \mathcal{R}(\Phi_R) O(\Phi_R) - \sum_{\{ij\}} \mathcal{D}_{ij}^{(S)}(\Phi_R) O(b_{ij}(\Phi_R)) \right]$$

- ▶ Different observable dependence in  $\mathcal{R}$  and  $\mathcal{D}$  but if showered separately  $\Rightarrow$  "double counting" ✗

## Solution: Let's in the following ...

- ▶ rewrite  $\langle O \rangle^{(\text{NLO})}$  a bit
- ▶ add some PS resummation into the game leading to  $\langle O \rangle^{(\text{NLO+PS})}$  and claim that:
  - ▶  $\langle O \rangle^{(\text{NLO+PS})} = \langle O \rangle^{(\text{NLO})}$  to  $\mathcal{O}(\alpha_s)$
  - ▶  $\langle O \rangle^{(\text{NLO+PS})}$  contains the first step of a PS evolution which can then be continued trivially with a regular PS
- ▶ sketch how  $\langle O \rangle^{(\text{NLO+PS})}$  is being generated in MC@NLO and POWHEG

## From fixed order to resummation

First rewrite: Additional set of subtraction terms  $\mathcal{D}^{(A)}$ 

$$\langle O \rangle^{(\text{NLO})} = \sum_{\vec{f}_B} \int d\Phi_B \bar{\mathcal{B}}^{(A)}(\Phi_B) O(\Phi_B) + \sum_{\vec{f}_R} \int d\Phi_R \left[ \mathcal{R}(\Phi_R) O(\Phi_R) - \sum_{\{ij\}} \mathcal{D}_{ij}^{(A)}(\Phi_R) O(b_{ij}(\Phi_R)) \right]$$

with  $\bar{\mathcal{B}}^{(A)}(\Phi_B)$  defined as:

$$\bar{\mathcal{B}}^{(A)}(\Phi_B) = \mathcal{B}(\Phi_B) + \tilde{\mathcal{V}}(\Phi_B) + \sum_{\{\tilde{ij}\}} \mathcal{I}_{\tilde{ij}}^{(S)}(\Phi_B) + \sum_{\{\tilde{ij}\}} \sum_{f_i=q,g} \int d\Phi_{R|B}^{ij} \left[ \mathcal{D}_{ij}^{(A)}(r_{\tilde{ij}}(\Phi_B)) - \mathcal{D}_{ij}^{(S)}(r_{\tilde{ij}}(\Phi_B)) \right]$$

- ▶  $\mathcal{D}_{ij}^{(A)}$  must have same kinematics mapping as  $\mathcal{D}_{ij}^{(S)}$
- ▶ Exact choice of  $\mathcal{D}_{ij}^{(A)}$  will later specify MC@NLO vs. POWHEG
- ▶ Issue with different observable kinematics not yet solved → next step

## From fixed order to resummation

## Second rewrite: Make observable correction term explicit

$$\begin{aligned}
\langle O \rangle^{(\text{NLO})} &= \sum_{\vec{f}_B} \int d\Phi_B \mathcal{B}^{(\text{A})}(\Phi_B) O(\Phi_B) \\
&\quad + \sum_{\vec{f}_R} \int d\Phi_R \left[ \mathcal{R}(\Phi_R) - \sum_{\{ij\}} \mathcal{D}_{ij}^{(\text{A})}(\Phi_R) \right] O(\Phi_R) \\
&\quad + \langle O \rangle^{(\text{corr})}
\end{aligned}$$

with  $\langle O \rangle^{(\text{corr})}$  defined as:

$$\langle O \rangle^{(\text{corr})} = \sum_{\vec{f}_R} \int d\Phi_R \sum_{\{ij\}} \mathcal{D}_{ij}^{(\text{A})}(\Phi_R) \left[ O(\Phi_R) - O(b_{ij}(\Phi_R)) \right]$$

- ▶ Explicit correction term due to observable kinematics:  $\langle O \rangle^{(\text{corr})}$
- ▶ Essence of NLO+PS
  - ▶ Ignore  $\langle O \rangle^{(\text{corr})}$  for the time being
  - ▶ Apply PS resummation to first line using  $\Delta^{(\text{A})}$  in which  $\mathcal{D}^{(\text{PS})} \rightarrow \mathcal{D}^{(\text{A})}$

## From fixed order to resummation

## Master formula for NLO+PS up to first emission

$$\begin{aligned}
\langle O \rangle^{(\text{NLO+PS})} = & \sum_{\vec{f}_B} \int d\Phi_B \bar{\mathcal{B}}^{(A)}(\Phi_B) \left[ \underbrace{\Delta^{(A)}(t_0)}_{\text{unresolved}} O(\Phi_B) \right. \\
& + \left. \sum_{\{\vec{i}\vec{j}\}} \sum_{f_i} \int_{t_0} d\Phi_{R|B}^{ij} \underbrace{\frac{\mathcal{D}_{ij}^{(A)}(r_{\vec{i}\vec{j}}(\Phi_B))}{\mathcal{B}(\Phi_B)} \Delta^{(A)}(t)}_{\text{resolved, singular}} O(r_{\vec{i}\vec{j}}(\Phi_B)) \right] \\
& + \sum_{\vec{f}_R} \int d\Phi_R \left[ \underbrace{\mathcal{R}(\Phi_R) - \sum_{ij} \mathcal{D}_{ij}^{(A)}(\Phi_R)}_{\text{resolved, non-singular}} \right] O(\Phi_R)
\end{aligned}$$

- ▶ This is generated in the following way:
  - ▶ Generate seed event according to first or second line of  $\langle O \rangle^{(\text{NLO})}$  on last slide
  - ▶ Second line:  $\mathbb{H}$ -event with  $\Phi_R$  is kept as-is  $\rightarrow$  resolved, non-singular term
  - ▶ First line:  $\mathbb{S}$ -event with  $\Phi_B$  is processed through one-step PS with  $\Delta^{(A)}$   
 $\Rightarrow$  emission (resolved, singular) or no emission (unresolved) above  $t_0$
- ▶ To  $\mathcal{O}(\alpha_s)$  this reproduces  $\langle O \rangle^{(\text{NLO})}$  **including the correction term**
- ▶ Resolved cases: Subsequent emissions can be generated by ordinary PS

## Special case: MC@NLO

Choice of  $\mathcal{D}^{(A)}$ 

- ▶ Choose the additional subtraction terms as

$$\mathcal{D}_{ij}^{(A)} \rightarrow \mathcal{D}_{ij}^{(S)}$$

## Comments

- ▶  $\bar{\mathcal{B}}^{(A)}$  simplified significantly
- ▶ Still non-trivial to implement, need either of:
  - ▶ One-step PS algorithm based on subtraction terms  $\mathcal{D}_{ij}^{(S)}$ 
    - ! splitting kernels can become negative  $\Rightarrow \Delta > 1$  !
  - ▶ ME subtraction using ordinary PS kernels  $\mathcal{D}_{ij}^{(PS)}$ 
    - ! soft divergences (subleading in  $\frac{1}{N_C}$ ) not covered !
- ▶ In SHERPA's MC@NLO implementation:
  - ▶  $\mathcal{D}^{(S)}$  from Catani-Seymour
  - ▶ Weighted  $N_C = 3$  one-step PS to generate  $\Delta > 1$

## Special case: POWHEG

## Original POWHEG

- ▶ Choose additional subtraction terms as

$$\mathcal{D}_{ij}^{(A)}(\Phi_R) \rightarrow \rho_{ij}(\Phi_R) \mathcal{R}(\Phi_R) \quad \text{where} \quad \rho_{ij}(\Phi_R) = \frac{\mathcal{D}_{ij}^{(S)}(\Phi_R)}{\sum_{mn} \mathcal{D}_{mn}^{(S)}(\Phi_R)}$$

- ▶  $\mathbb{H}$ -term vanishes
- ▶  $\bar{\mathcal{B}}^{(A)}$  remains complicated now, includes real-emission integration (may be done by Monte-Carlo method)
- ▶ Similar to PS with ME-correction for 1st emission (e.g. Herwig, Pythia)

## Mixed scheme

- ▶ Subtract arbitrary regular piece from  $\mathcal{R}$  and generate separately

$$\mathcal{D}_{ij}^{(A)}(\Phi_R) \rightarrow \rho_{ij}(\Phi_R) [\mathcal{R}(\Phi_R) - \mathcal{R}^r(\Phi_R)] \quad \text{where} \quad \rho_{ij} \text{ as above}$$

- ▶ Allows to generate the non-singular cases of  $\mathcal{R}$  without underlying  $\mathcal{B}$
- ▶ More control over how much is exponentiated

## Subtleties to note

## Exponentiation uncertainty

- ▶ Have to exponentiate full subtraction terms  $\mathcal{D}_{ij}^{(S)}$  (MC@NLO) or even  $\mathcal{R}$  (POWHEG) for NLO accuracy
- ▶ Exponent contains arbitrary terms beyond all-orders singular pieces  
= Systematic theory uncertainty in NLO+PS

⇒ Studied in detail in Results later

## Renormalisation scale choice in NLO vs. PS

- ▶ First emission partly done by NLO matrix element, partly by PS
- ▶  $\alpha_s^{(\text{NLO})}(\mu_R)$  taken at fixed scale
- ▶  $\alpha_s^{(\text{PS})}(k_\perp)$  taken at transverse momentum of the branching (partially resums soft higher-order contributions)

⇒ Only noted here without solution, critical for smooth NLO $\otimes$ NLO merging

## NLO+PS uncertainties

### Perturbative uncertainties

- ▶ Unknown higher-order corrections
- ▶ Estimated here by simultaneous scale variations

$$\mu_F = \mu_R = \frac{1}{2}\mu \dots 2\mu$$

↪  $pp \rightarrow h + \text{jet}$  later

### Non-perturbative uncertainties

- ▶ Model uncertainties in hadronisation, hadron decays, multiple parton interactions
- ▶ Estimated here by variation of parameters/models within tuned ranges

↪  $pp \rightarrow W + \text{jet}$  later

### Exponentiation uncertainties

- ▶ Arbitrariness of  $\mathcal{D}^{(A)}$  and thus of the exponent in  $\Delta^{(A)}$
- ▶ Estimated here using SHERPA by:
  - ▶ Comparing MC@NLO and POWHEG
  - ▶ Using MC@NLO with variable “dipole  $\alpha_{\text{cut}}$ ” restriction in  $\mathcal{D}^{(S)}$ :  
 $\alpha_{\text{cut}} \rightarrow 0$  decreases phase space for non-singular contributions

## Exponentiation uncertainties in the example of $gg \rightarrow h$

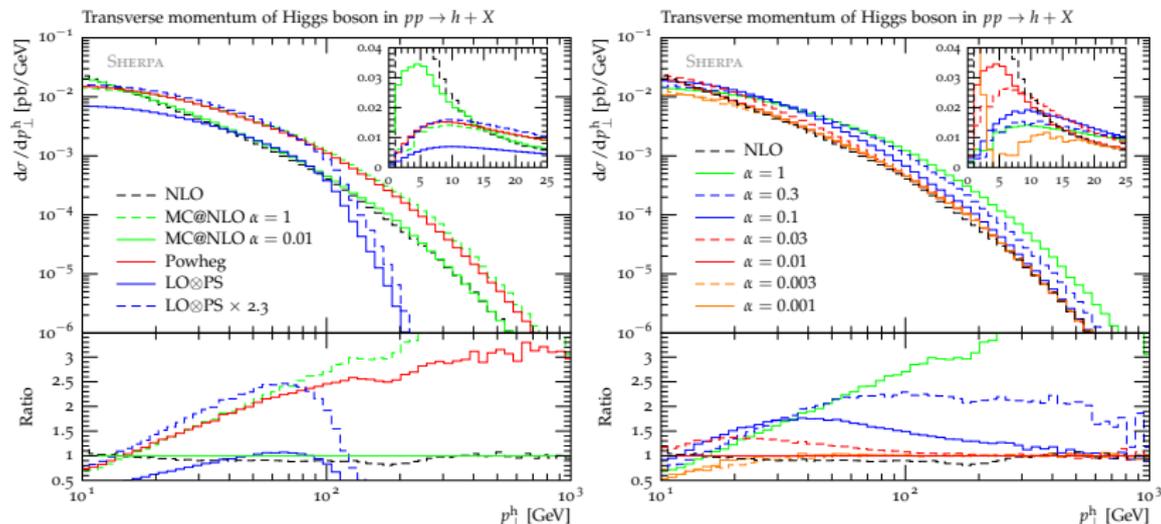
### Example setup

- ▶  $gg \rightarrow h \rightarrow \tau\tau$  at LHC with  $\sqrt{s} = 7$  TeV and  $m_h = 120$  GeV,  $\mu = m_h$
- ▶ Analysed with  $p_{\perp}^{\tau} > 25$  GeV and  $|n^{\tau}| < 3.5$
- ▶ Jets defined using inclusive  $k_{\perp}$  with  $R = 0.7$  and  $p_{\perp} > 20$  GeV

### Studies at parton shower level

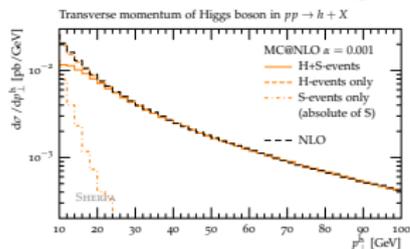
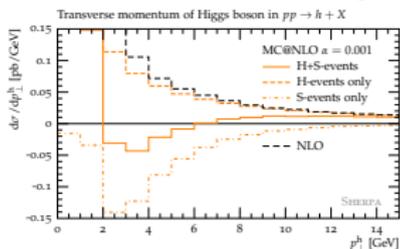
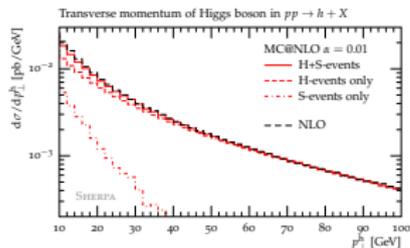
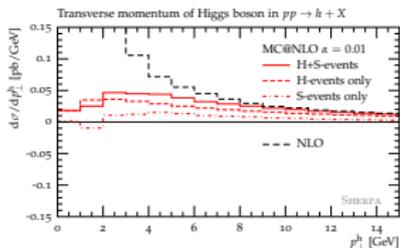
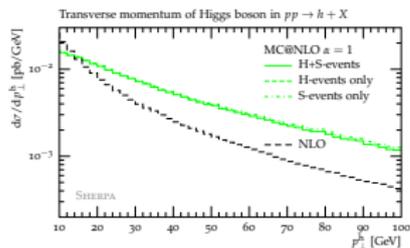
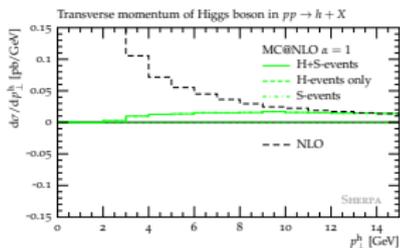
1. Validate NLO+PS against fixed NLO predictions
2. Comparison with LO parton shower (LO+PS)
3. MC@NLO vs. POWHEG
4. MC@NLO with  $0.001 \leq \alpha_{\text{cut}} \leq 1$  variation

⇒ Very busy plots  
(SORRY!)

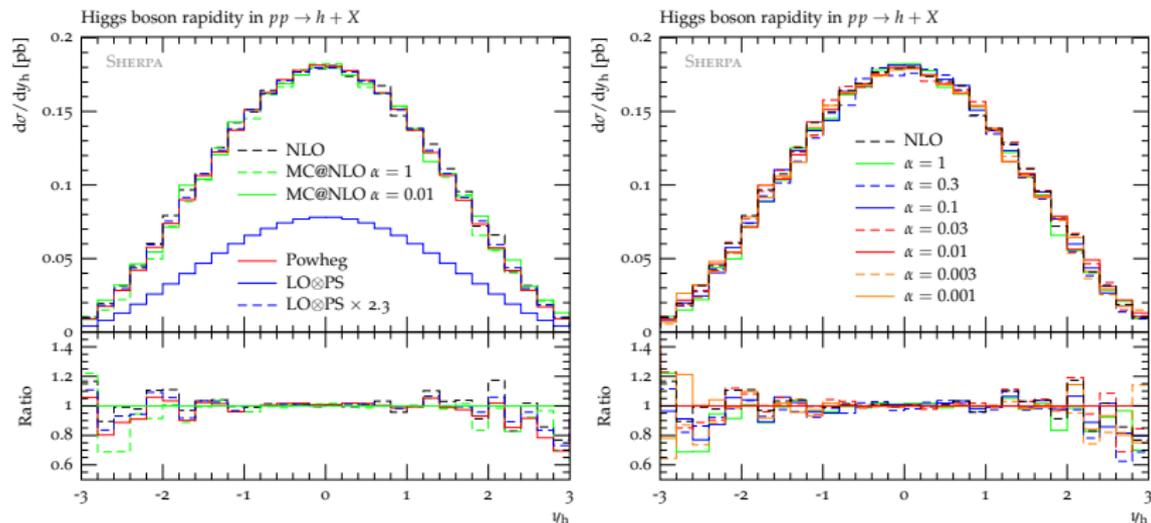
Exponentiation uncertainties in the example of  $gg \rightarrow h$ 

- ▶ Surprising result: Huge NLO+PS uncertainties especially at large  $p_{\perp}^h$
- ▶ POWHEG and unrestricted MC@NLO similar
- ▶ Decreasing exponentiation of non-singular pieces with  $\alpha_{\text{cut}} \lesssim 0.01$  recovers NLO behaviour
- ▶ Resummation region  $p_{\perp}^h \rightarrow 0$  strongly affected by  $\alpha_{\text{cut}}$  variation: side effect of imperfect functional form of  $\alpha$  (vs. parton shower  $t \sim k_{\perp}^2$ )

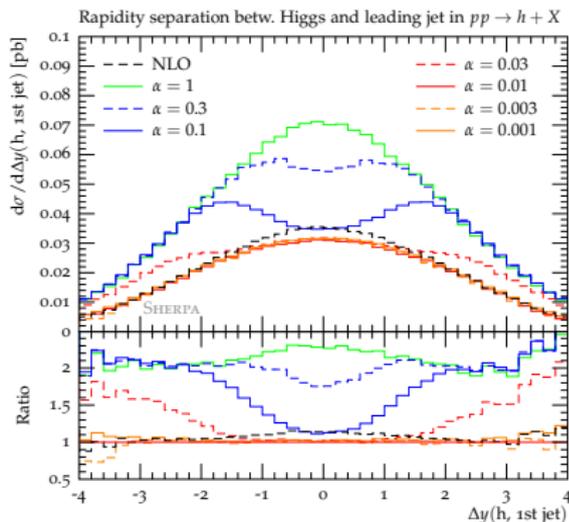
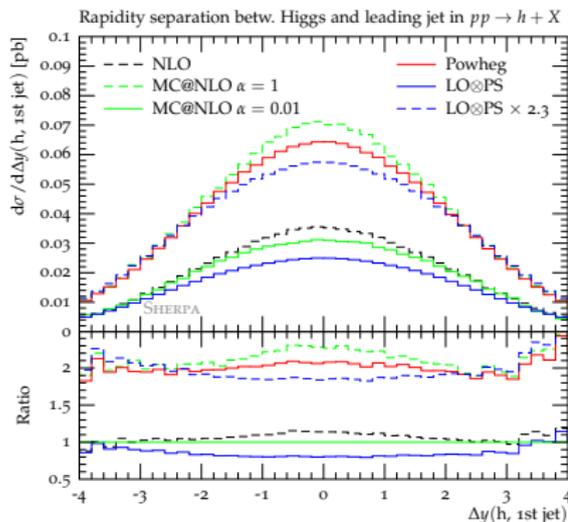
# Exponentiation uncertainties in the example of $gg \rightarrow h$



- Predictions separated by  $\mathbb{H}$  and  $\mathbb{S}$  events for illustration purposes

Exponentiation uncertainties in the example of  $gg \rightarrow h$ 

- ▶ Predictions much more stable for  $y_h$  than for  $p_{\perp}^h$
- ▶ Observable already exists at LO, thus described at NLO here

Exponentiation uncertainties in the example of  $gg \rightarrow h$ 

- ▶ Large uncertainties for  $\Delta y(h, j)$
- ▶ Interesting dip structure in MC@NLO due to cuts on exponentiated phase space  
Surprisingly similar to effect from dead zones in MC@NLO with HERWIG

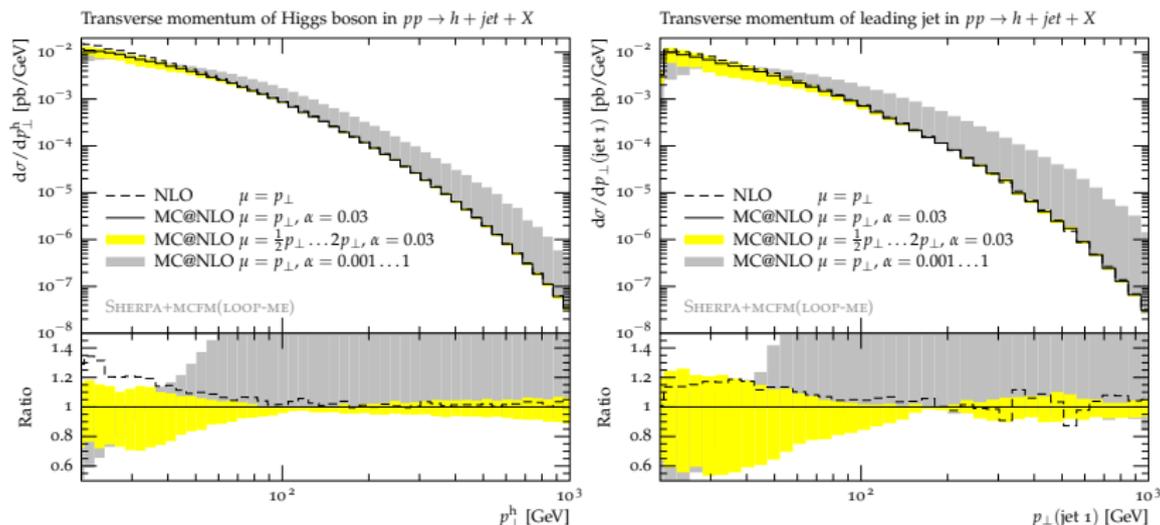
## Predictions for $pp \rightarrow h + \text{jet}$

### Example setup

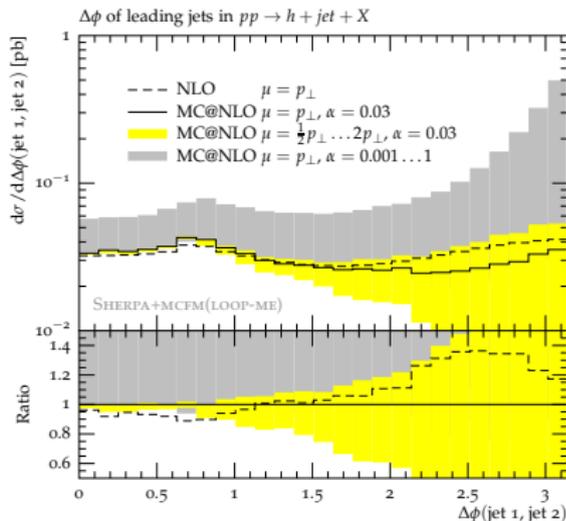
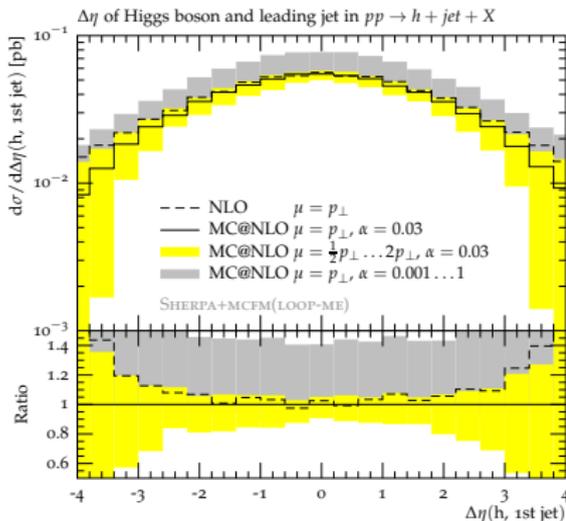
- ▶  $pp \rightarrow h[\rightarrow \tau\tau] + \text{jet}$  at LHC with  $\sqrt{s} = 7$  TeV and  $m_h = 120$  GeV,  $\mu = p_{\perp}^{\text{lead}}$
- ▶ Virtual matrix element interfaced from MCFM
- ▶ Generated ME level with  $p_{\perp} > 10$  GeV for inclusive  $k_{\perp}$  jets with  $R = 0.5$
- ▶ Analysed with  $p_{\perp}^{\tau} > 25$  GeV and  $|n^{\tau}| < 3.5$ , jets defined using inclusive  $k_{\perp}$  with  $R = 0.7$  and  $p_{\perp} > 20$  GeV

### Studies

- ▶ Includes hadronisation, hadron decays, multiple parton interactions (MPI), QED corrections to  $h \rightarrow \tau\tau$  decay
- ▶ Scale uncertainty band (yellow) from  $\mu_F = \mu_R = \frac{1}{2}\mu \dots 2\mu$
- ▶ Exponentiation uncertainty band (gray) from  $\alpha_{\text{cut}} = 0.001 \dots 1$

Predictions for  $pp \rightarrow h + jet$ 

- ▶ Despite NLO accuracy, large exponentiation uncertainty for large  $p_{\perp}$ :
  - ▶ Large influence from higher-order corrections in  $\Delta$  where more phase space is exponentiated
  - ▶ Additional distortion from scale difference for real-emission: relative  $p_{\perp}$  of partons vs.  $p_{\perp}$  against beam

Predictions for  $pp \rightarrow h + \text{jet}$ 

- ▶ Milder exponentiation variations in  $\Delta\eta(\text{h, jet})$ , mainly normalisation due to larger emission rates with  $\alpha_{\text{cut}} \rightarrow 1$
- ▶  $\Delta\phi(\text{jet 1, jet 2})$ : Back-to-back situation amplified due to harder radiation

## Non-perturbative effects in $W + \text{jet}$ production

### Example setup

- ▶  $pp \rightarrow W[\rightarrow e\nu] + \text{jet}$  at LHC with  $\sqrt{s} = 7 \text{ TeV}$ ,  $\mu = p_{\perp}^{\text{lead}}$
- ▶ Virtual matrix element interfaced from BlackHat
- ▶ Exponentiation level fixed at  $\alpha_{\text{cut}} = 0.03$
- ▶ Generated ME level with  $p_{\perp} > 10 \text{ GeV}$  for inclusive  $k_{\perp}$  jets with  $R = 0.5$
- ▶ Analysed jets with  $p_{\perp} > 20 \text{ GeV}$  for inclusive  $k_{\perp}$  jets with  $R = 0.7$

### Non-perturbative effects

#### “Parton Level”

Only seed event + first emission off  $\mathbb{S}$ -events in MC@NLO

#### “Shower Level”

PL + all QCD emissions in the parton shower and QED emissions in the YFS approach

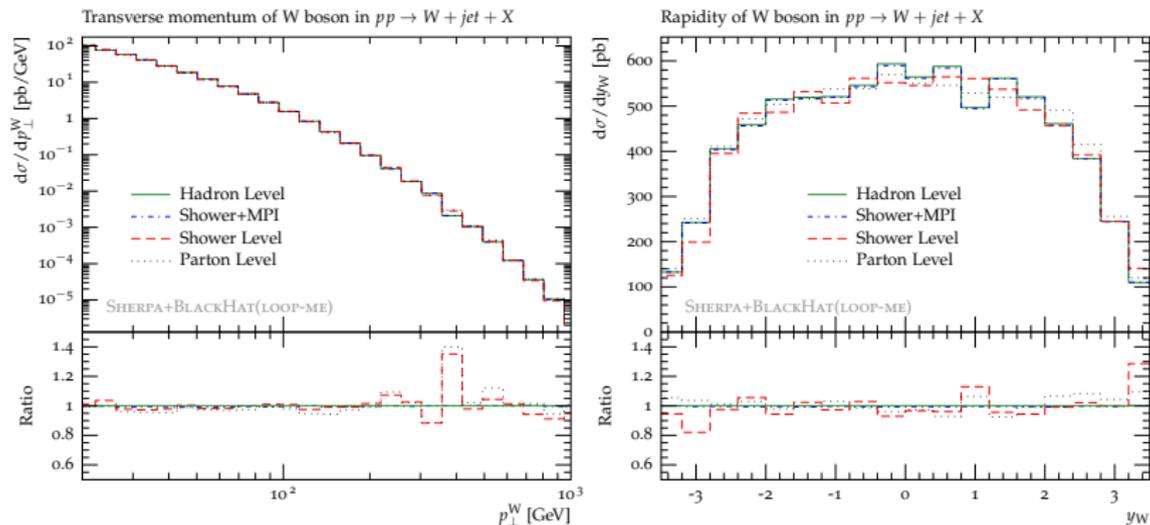
#### “Shower+MPI”

SL + multiple parton interactions and intrinsic  $p_{\perp}$  of the beam hadron

#### “Hadron Level”

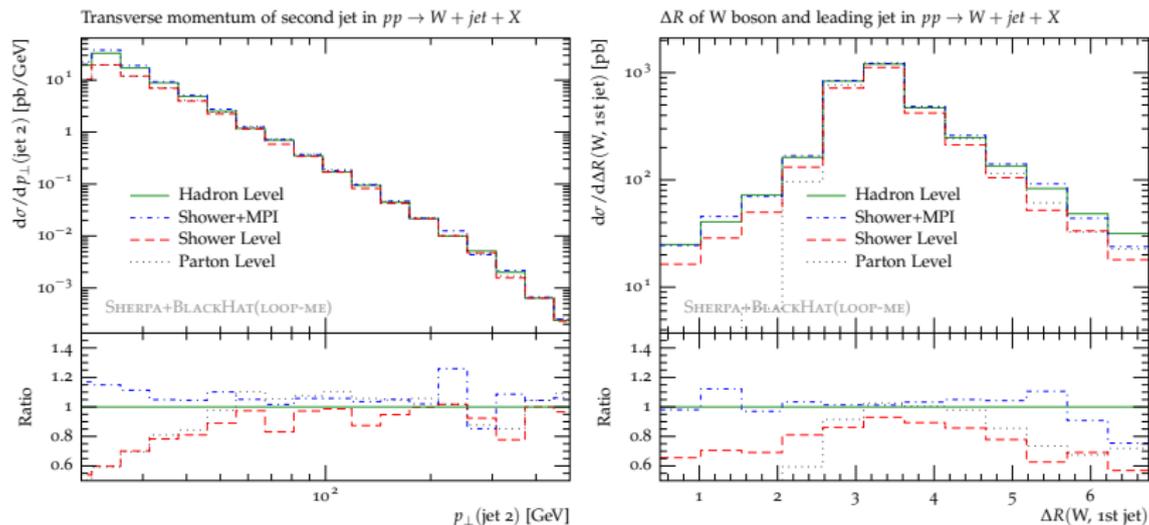
Additionally, hadronisation and hadron decays are included

# Non-perturbative effects in $W + \text{jet}$ production



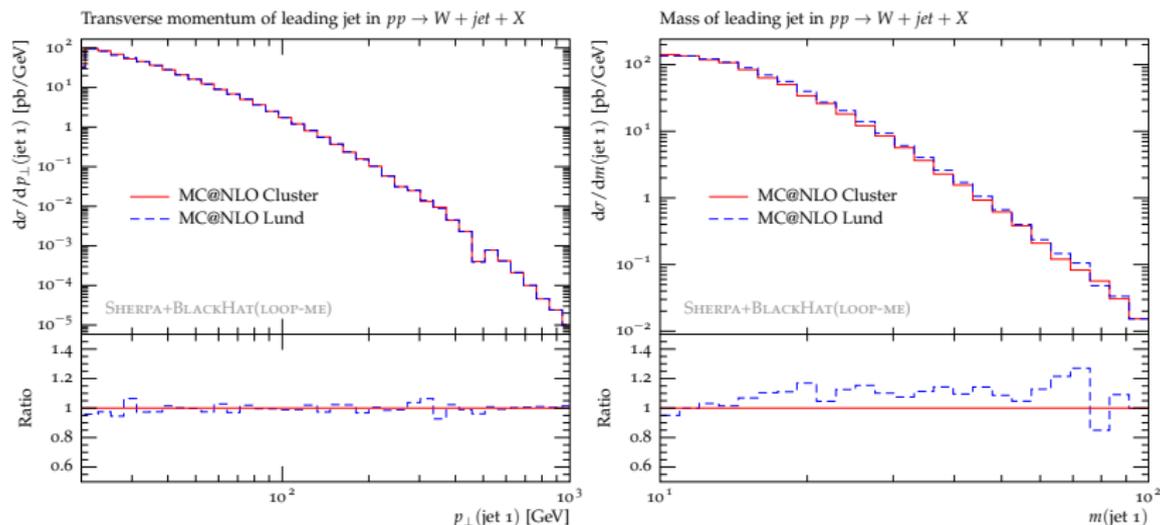
- Properties of the  $W$ -boson virtually unaffected

# Non-perturbative effects in $W + \text{jet}$ production



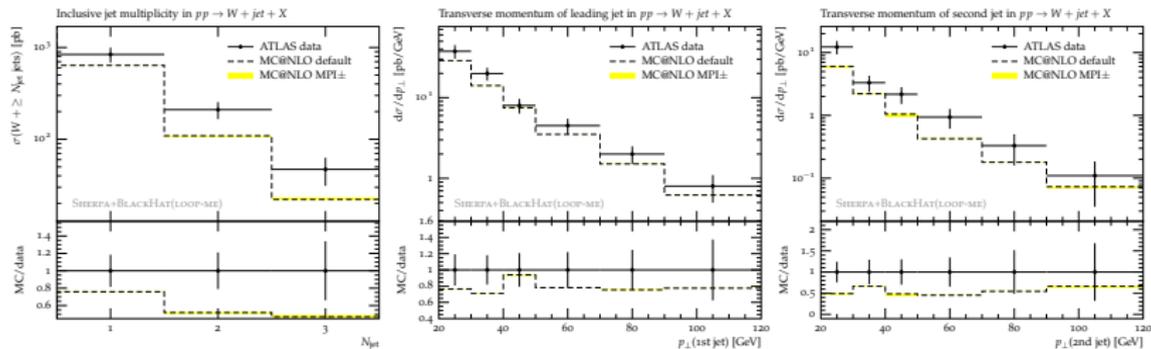
- ▶ Jet properties changed significantly by non-perturbative effects
  - ▶ Hadronisation and MPI partially compensate each other, depends on jet algorithm
- ⇒ How large is the uncertainty?

# Hadronisation uncertainties in $W + \text{jet}$ production



- ▶ Probe hadronisation uncertainties by switching from SHERPA default cluster fragmentation to Lund string
- ▶ Differences negligible for all jet observables studied, except the specifically sensitive jet mass

# Comparison to data for $W + \text{jet}$ production



- ▶ Comparison to ATLAS data (arXiv:1012.5382):  
Good agreement in shape, discrepancies in jet rates
- ▶ Especially two/three jet rates too low: Only predicted at LO/PS
- ▶ MPI parameter variations plotted as yellow band  $\Rightarrow$  negligible

## Comparison to data for $Z + \text{jet}$ production

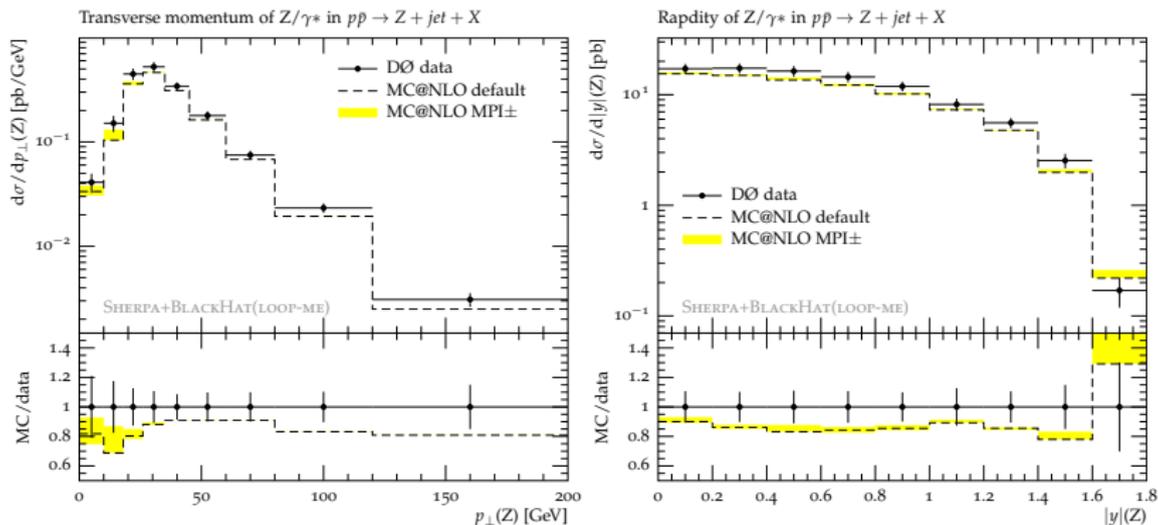
### Example setup

- ▶  $pp \rightarrow Z + \text{jet}$  at Tevatron with  $\sqrt{s} = 1.96 \text{ TeV}$ ,  $\mu = p_{\perp}^{j_{\text{lead}}}$
- ▶ Virtual matrix element interfaced from BlackHat
- ▶ Exponentiation level fixed at  $\alpha_{\text{cut}} = 0.03$
- ▶ Generated ME level with  $p_{\perp} > 10 \text{ GeV}$  for inclusive  $k_{\perp}$  jets with  $R = 0.5$

### Tevatron analyses

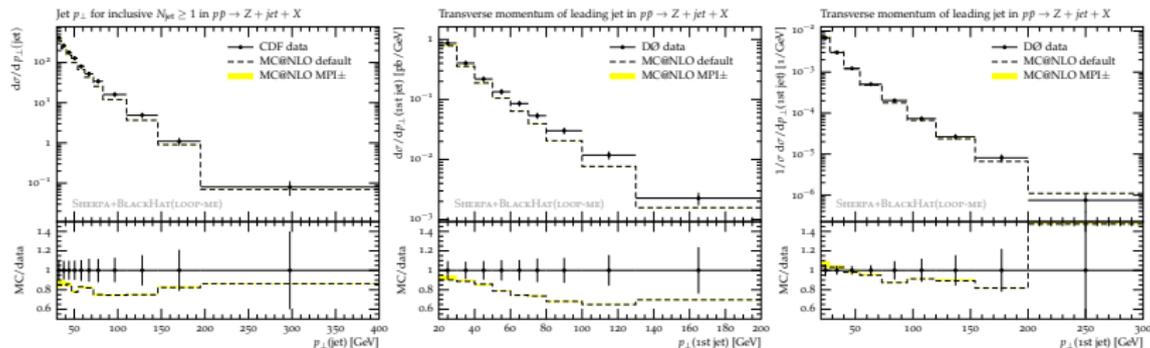
- ▶ CDF  $Z + \text{jets}$  arXiv:0711.3717
- ▶ DØ  $Z + \text{jet}$  arXiv:0808.1296
- ▶ DØ  $Z + \text{jets}$  arXiv:0903.1748
- ▶ DØ  $Z + \text{jet}$  arXiv:0907.4286

# Comparison to data for $Z + \text{jet}$ production



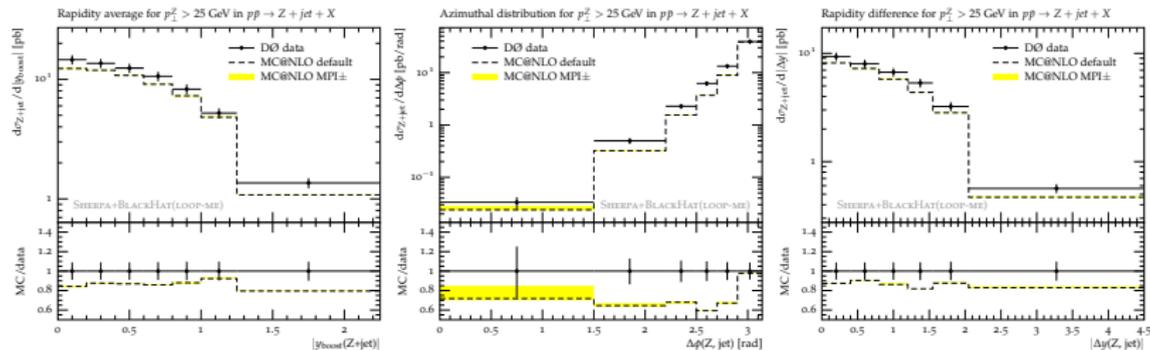
- ▶  $Z$ -boson properties in  $Z + \text{jet} + X$  production
- ▶ Fair agreement, 10% rate deficiency
- ▶ MPI uncertainties largest at low  $p_{\perp}(Z)$

# Comparison to data for $Z + \text{jet}$ production



- ▶ One-jet-rate too low by 10-20%
- ▶ Not conclusive on shape of leading jet  $p_{\perp}$
- ▶ Reminder: Large exponentiation uncertainties

## Comparison to data for $Z + \text{jet}$ production



- ▶ Angular correlations of  $Z$ -boson and leading jet
- ▶ Shape of rapidity distributions matched fairly well
- ▶ Significant deviations for azimuthal correlation:  
Back-to-back works, but  $\Delta\phi < \pi$  is underestimated.  
That region is generated by emissions beyond the first one  $\Rightarrow$  only LO/PS accuracy

## Summary

- ▶ NLO+PS matching was presented in common formalism
- ▶ POWHEG and MC@NLO developed as special cases
- ▶ Uncertainties from exponentiation ambiguities are large but understood
- ▶ Scale and non-perturbative uncertainties relatively small
- ▶ First NLO+PS predictions for  $h + \text{jet}$
- ▶  $W/Z + \text{jet}$  compared to experimental data

## Outlook

- ▶ Improved functional form of dipole  $\alpha$  could allow for better limitation of exponentiation
- ▶ Merging NLO+PS with higher-multiplicity tree-level MEs can provide better description of multi-jet final states ( $\rightarrow$  e.g. MENLOPS)
- ▶ Ultimate goal: Merging of NLO at different multiplicities + parton shower